

CHAPTER-15

PERIMETER AND AREA

Question 1.

A rectangular park is 55 m wide and 89 m long. Find the cost of fencing it at the rate of ₹ 22.50 per 100 metres.

Solution:

Length 89 m and Breadth = 55 m

∴ Perimeter of a rectangle

$$= 2 \times [\text{Length} + \text{Breadth}]$$

Perimeter of the rectangular park

$$= 2[89 \text{ m} + 55 \text{ m}] = 2[144 \text{ m}] = 288 \text{ m}$$

∴ Length of the wire = 288 m

∴ Cost of fencing

$$= [\text{Perimeter}] \times [\text{Cost of fencing}]$$

$$= [288 \text{ m}] \times [\text{₹}22.50 \text{ per } 100 \text{ metre}]$$

$$= \text{₹ } 288 \times 22510 \times 1100 = \text{₹ } 64.80$$

Question 2.

Which has a greater perimeter: a square plot of side 75 m or a rectangular plot with sides 100 m and 65 m and by how much?

Solution:

∴ Perimeter of a square = $4 \times \text{Side}$

$$\therefore \text{Perimeter of the square plot} = 4 \times 75 \text{ m} = 300 \text{ m}$$

On the other hand, perimeter of rectangle = $2 \times [\text{Length} + \text{Breadth}]$

$$\therefore \text{Perimeter of the given rectangular plot} = 2[100 \text{ m} + 65 \text{ m}] = 2[165 \text{ m}] = 330 \text{ m}$$

$$\therefore 330 \text{ m} > 300 \text{ m} \text{ and } 330 \text{ m} - 300 \text{ m} = 30 \text{ m}$$

∴ The perimeter of the rectangular plot is more than square plot by 30 m.

Question 3.

What would be the cost of fencing a rectangular park whose length is 150 m and breadth is 120 m if the fence costs ₹ 40 per meter?

Solution:

The length of the fence is the perimeter of the rectangular park.

Given that the length of the rectangular park = 150 m and breadth = 120 m

$$\therefore \text{Perimeter} = 2(l + b)$$

$$= 2(150 + 120)$$

$$= 2(270)$$

$$= 540 \text{ m}$$

Now cost of fencing per meter = ₹ 40

$$\text{Cost of fencing the rectangular park} = \text{₹ } 40 \times 540 = \text{₹ } 21600$$

Question 4.

A piece of string is 36 cm long. What will be the length of each side, if it is used to form:

(a) A square,

(b) A triangle with all sides of equal length, and

(c) A hexagon (a six-sided closed figure) with sides of equal length?

Solution:

(a) Given, a piece of string is 36 cm long

\therefore length of each side of the square = a

perimeter = 36

$\Rightarrow 4a = 36$

$\Rightarrow a = 9$ cm

(b) Length of each side of the triangle = $3a$ (Given)

perimeter = 36

$\Rightarrow 3a = 36$

$\Rightarrow a = 12$ cm

(c) Length of each side of hexagon = a

perimeter = 36

$\Rightarrow 36 = 6a$

$\Rightarrow a = 6$ cm

Question 5.

Find out the total distance Akshi has covered in 5 rounds.

Solution:

Distance covered by Akshi in 5 rounds = $5 \times$ perimeter of PQRS

$= 5 \times 220$

$= 1100$ m

Question 6.

Find out the total distance Toshi has covered in 7 rounds. Who ran a longer distance?

Solution:

Distance covered by Toshi in 7 rounds = $7 \times 180 = 1260$ m

$\therefore 1260$ m $>$ 1100 m

Hence Toshi ran the longer distance.

Question 7.

The area of a rectangular garden 25 m long is 300 sq m. What is the width of the garden?

Solution:

Given, area of rectangular garden = 300 sq.m

and length = 25 m

area of rectangular field = $l \times b$

$\Rightarrow 300 = 25 \times b$

$\Rightarrow b = 12$ m

Question 8.

What is the cost of tiling a rectangular plot of land 500 m long and 200 m wide at the rate of ₹ 8 per hundred sq m?

Solution:

Here, length = 500 m and breadth = 200 m

Hence the area of the rectangular plot = length \times breadth

$$= 500 \times 200$$

$$= 1,00,000 \text{ m}^2$$

Now cost of tilling a rectangular plot = $\frac{8}{100}$

Hence the cost of tilling 1,00,000 sq. m of rectangular plot = $\frac{8}{100} \times 100000 = ₹ 8,000$

Question 9.

A rectangular coconut grove is 100 m long and 50 m wide. If each coconut tree requires 25 sq m, what is the maximum number of trees that can be planted in this grove?

Solution:

Area of rectangular coconut grove = $100 \times 50 = 5000 \text{ sq. m}$

Given each coconut tree requires 25 sq. m

then the maximum no. of trees that can be planted in this grove = $5000/25 = 200$

Question 10.

Explore and figure out how many pieces have the same area.

Solution:

There are two pieces (A and B) that have the same area.

Question 11.

How many times bigger is Shape D as compared to Shape C? What is the relationship between Shapes C, D, and E?

Solution:

Shape D is two times bigger than shape C. Clearly from the figure, the area of shapes C and E is equal to the area of shape D.

Question 12.

Which shape has more area: Shape D or F? Give reasons for your answer.

Solution:

Since the medium triangle and the square are each made up of two small tangram triangles, they each have an area $2x$ that of the small triangle. Hence both have the same area.

Question 13.

Which shape has more area: Shape F or G? Give reasons for your answer.

Solution:

Since the medium triangle and the rhomboid are each made up of two small tangram triangles, they each have an area $2x$ that of the small triangle. Hence both have the same area.

Question 14.

What is the area of Shape A as compared to Shape G? Is it twice as big? Four times

as big?

[Hint: In the tangram pieces, by placing the shapes over each other, we can find out that Shapes A and B have the same area, and Shapes C and E have the same area. You would have also figured out that Shape D can be exactly covered using Shapes C and E, which means Shape D has twice the area of Shape C or Shape E, etc.]

Solution:

Shape A has twice the area of shape G.

Question 15.

Give the dimensions of a rectangle whose area is the sum, of the areas of these two rectangles having measurements: $5\text{ m} \times 10\text{ m}$ and $2\text{ m} \times 7\text{ m}$.

Solution:

Here, Area of rectangle 1 = $5 \times 10 = 50\text{ sq m}$

Area of rectangle 2 = $2 \times 7 = 14\text{ sq m}$

The Sum of the areas of these 2 rectangles = $50 + 14 = 64\text{ sq m}$

Now, the total area of the rectangle = 64

Let's say the sides of the rectangle are Length = x and Width = y

Area of rectangle = $x \times y$

Hence $x \times y = 64$

$xy = 64$

Let's say $x = 1$, then $y = 64/1 = 64$

if $x = 2$, then $y = 64/2 = 32$

Hence the dimensions of the rectangle are (1×64) , (2×32)

Question 16.

The area of a rectangular garden that is 50 m long is 1000 sq m. Find the width of the garden.

Solution:

Width of rectangular garden = area / length of garden

= $1000/50$

= 20 m